

SH-II/CSC/202/C4/18

B.Sc. Semester-II (Honours) Examination, 2018**COMPUTER SCIENCE (H)**

Subject Code : 21502

Course Code : SH/CSC/202/C4

Course Title : Discrete Structures

Time: 2 Hrs.

Full Marks: 40

*The figures in the margin indicate full marks.**Candidates are required to give their answers in their own words as far as practicable.*

1. Answer *any five* questions: 2×5=10
- What is countably infinite set?
 - What is Pigeonhole principle?
 - What is the use of asymptotic notations?
 - What is recurrence tree?
 - What do you mean by a graph?
 - What is Hamiltonian path?
 - What is tautology?
 - Express if-then operator (\rightarrow) in terms of the basic propositional operators (\vee , \wedge , \neg).
2. Answer *any four* questions: 5×4=20
- Explain bijective relation with an example. What is closure property?
 - Discuss big-oh (\mathcal{O}) and big-omega (Ω) notations with examples.
 - Solve the recurrence relation:
 $a_n = a_{n-1} + 2a_{n-2}$ with $a_0 = 2$ & $a_1 = 7$
 - Show that for any graph the number of odd-degree vertices is always even.
 - Write Kruskal's algorithm for finding MST.
 - What is Hamiltonian path and Hamiltonian circuit? Explain with example. 3+2=5
3. Answer *any one* question: 10×1=10
- In how many different ways can the letters of the word 'OPTICAL' be arranged so that the vowels come together? Using mathematical induction prove that $\forall n \geq 1, 8^n - 3^n$ is divisible by 5. 6+4=10
 - State and prove the propositional logic version of De Morgan's law for two variables.
Consider the following propositions:
 p : Mr A is smart
 q : Mr A is honest
Express the following statement in terms of p and q .
Mr. A is smart is necessary and sufficient for Mr A to be honest. 6+4=10